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## Extended reductive groups and representation theory.

An  $extended\ group$  for a connected reductive algebraic group G is a group fitting into an exact sequence

$$1 \to G \to {}^{\Sigma}G \to \Sigma \to 1$$
,

with  $\Sigma$  a finite group. I'll discuss first some old ideas for using such an extended group to keep track of representations of (real forms of) G. (The magic question is, "how do you tell a holomorphic discrete series from an antiholomorphic discrete series?") Then I'll discuss some problems arising in recent joint work with Lusztig about the representation theory of extended groups themselves.