February 27: Pavle Pandžić (University of Zagreb and Cornell), "Dirac operators on Harish-Chandra modules." FOLLOWED BY DINNER. In the 1970s,

Parthasarathy introduced a version of the Dirac operator D attached to a real reductive group, and used it to construct the discrete series representations. He also obtained a useful necessary condition, Dirac operator inequality, for unitarizability of an irreducible Harish-Chandra module.

In 1997 Vogan studied a purely algebraic version of D and used it to attach an invariant, called Dirac cohomology, to a Harish-Chandra module X. He conjectured that Dirac cohomology, if nonzero, determines the infinitesimal character of X. This conjecture was proved by Huang and myself in 2002. Subsequent generalizations to other settings were obtained by Kostant, Kumar, Alekseev-Meinrenken and Kac-Frajria-Papi. Further results on Dirac cohomology of Harish-Chandra modules included a relationship to  $\mathfrak n$  cohomology in some special cases (joint with Huang and Renard).

In this talk I will give a brief overview of the definitions and the above mentioned results. I will then describe some further ideas and open questions. The topics I plan to mention are algebraic Dirac induction,  $\mathfrak{p}^+$  cohomology of unitary highest weight modules, and sharpening the Dirac inequality.